## Activity: Happy and Unhappy Numbers

There are numbers that are called happy numbers. Here is the algorithm used to find them:

1. Pick a number $n$ you wish to test.
2. Let $n_{1}$ be the sum of the squares of the digits in number $n$.
3. Repeat step 2 until you reach: $0,1,4,16,20,37,42,58,89$, or 145 .
4. If you reached 1 , the number you started with is happy!

Numbers that are not happy are said to be sad or unhappy.

Example 1: Let's check if number 97 is happy:

$$
\begin{aligned}
& 97 \longrightarrow 9^{2}+7^{2}=81+49=130 \\
& 130 \longrightarrow 1^{2}+3^{2}+0^{2}=1+9+0=10 \\
& 10 \longrightarrow 1^{2}+0^{2}=1+0=1
\end{aligned}
$$

Number 97 is a happy number.

Problem 1: Check if the following numbers are happy or sad: 56, 556, 801, 937 and 961.

Challenge 1: The algorithm described above terminates when you reach $0,1,4,16,20,37,42,58,89$, or 145. Why? ()

Hint: Look at each of the termination numbers and check what would happen if you keep going.

Challenge 2: Write a computer program to test if a number is happy or not. Use this program to find all happy numbers between 0 and 1001.

